# IMPROVED (ALMOST) TIGHTLY-SECURE SIMULATION-SOUND QA-NIZK WITH APPLICATIONS

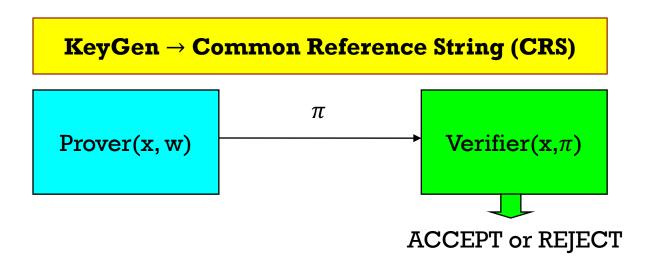
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Blum, Feldman, Micali 1988

#### NIZK PROOF SYSTEMS

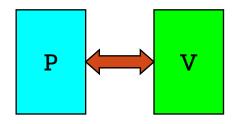
- Objective: To prove whether x ∈ NP language L without revealing its witness w
- Components:





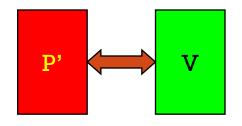
#### NIZK: PROPERTIES

#### Completeness



if  $x \in L$  then V accepts with 'high' probability

#### Soundness



if  $x \notin L$  then V rejects with 'high' probability, even with a cheating prover



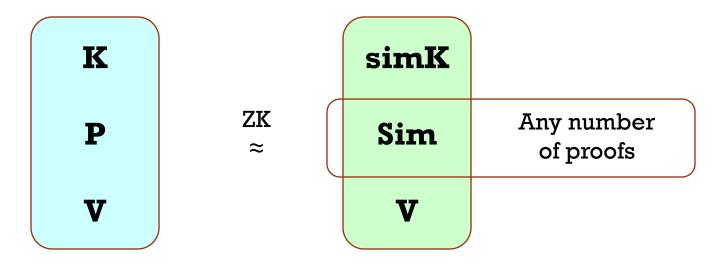
### ZERO-KNOWLEDGE

Proofs from adversary are sound

Proofs from adversary are sound



#### UNBOUNDED SIMULATION-SOUND NIZK

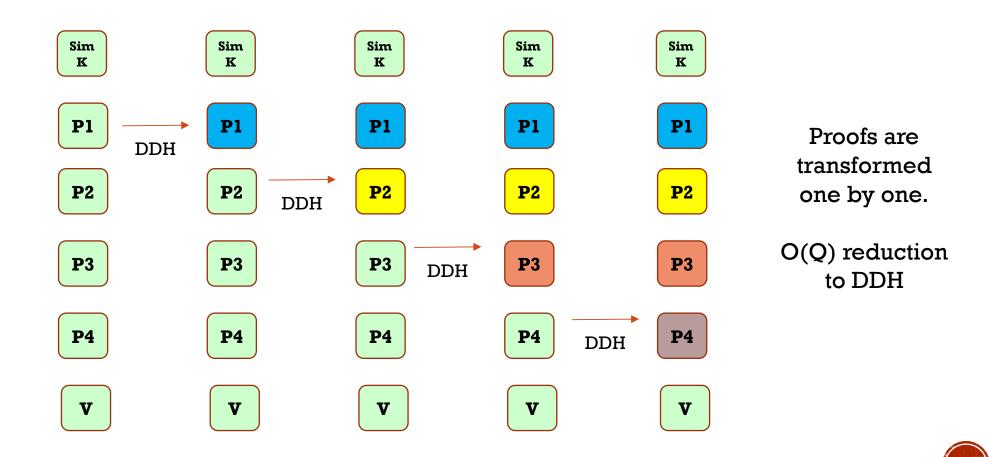


Proofs from adversary are sound

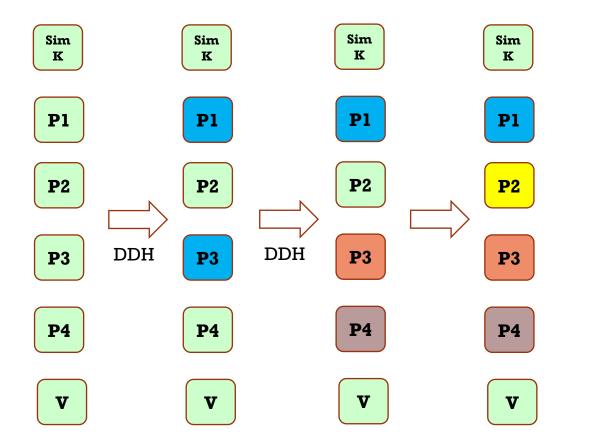
Proofs from adversary are sound



# (NON)-TIGHT SECURITY



# (ALMOST)-TIGHT SECURITY



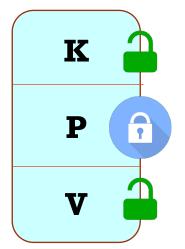
Many proofs are transformed in one go.

 $O(\lambda, \log Q)$  reduction to DDH.

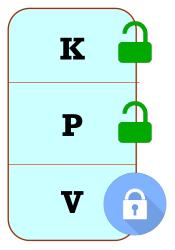


# WHY IS THIS CHALLENGING?

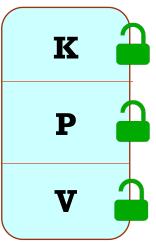
**Signatures** 



**PKEs** 



NIZK





# QUASI-ADAPTIVE NIZKS

#### **Smooth Projective Hash Functions [CS98]**

$$y = [Mx]$$
$$y^T = [x^T M^T]$$

Proj. Hash Key  $\lceil M^T K \rceil$ 

Public Hash

 $x^T[M^TK]$ 

Hash Key K

**Private Hash** 

CRSp  $[M^TK]_1$  Trapdoor K

 $y = [Mx]_1$  $y^T = [x^T M^T]_1$ 

**QA-NIZKs** 

CRSv  $[KA]_2, [A]_2$ 

Proof  $p = x^T [M^T K]_1$  $y^T K$ 

Simulator  $y^T K$ 

Verify  $y^T[KA]_2$  $= p[A]_2$ 



# USS-QA-NIZK

QA-NIZKs

$$y = [Mx]_1$$
$$y^T = [x^T M^T]_1$$

$$\begin{array}{c}
\text{Proof} \\
p = x^T [M^T K]_1
\end{array}$$



PR-MAC  $+[r^{T}(P_{0}+\tau P_{1})]_{1}, [r^{T}B^{T}]_{1}$ 

Non-tight O(Q) reduction

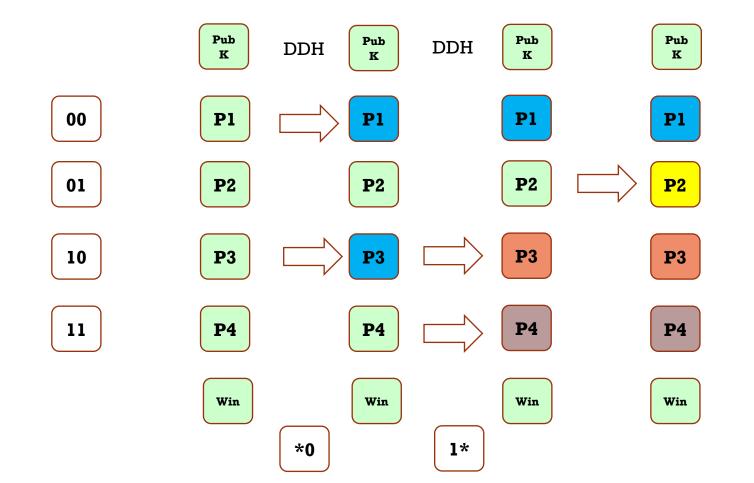


## TIGHTLY-SECURE USS-QA-NIZK

- [LPJY15] achieved this first
  - #proof independent of  $\lambda$
  - $O(\lambda)$  security reduction to DLIN
  - Public key size  $O(\lambda)$
  - Static partitioning [CW13, ...]
- We improve in the following ways
  - $O(\log Q)$  security reduction to any MDDH including SXDH
  - #Public key also independent of  $\lambda$
  - Adaptive partitioning [Hof17, used by: AHN+17, JOR18, GHKP18, ...]



#### ADAPTIVE PARTITIONING



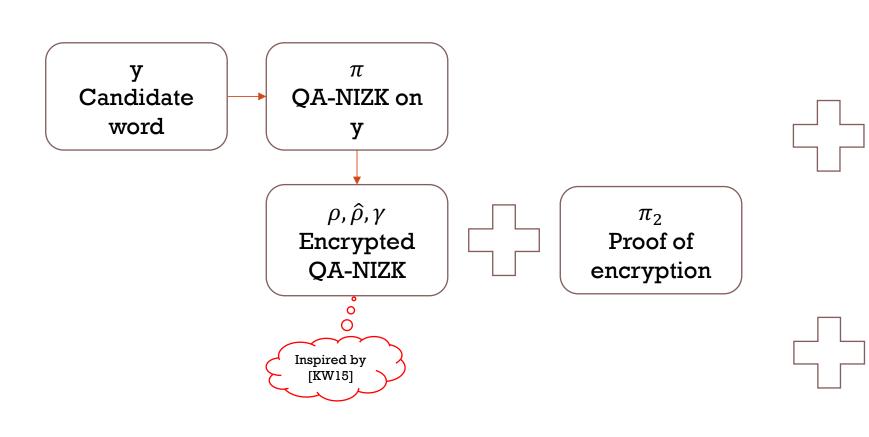


# TIGHT USS-QA-NIZK CONSTRUCTION

- Our AsiaCrypt version had a bug
- Jiaxin Pan discovered an attack and informed us
  - Thanks Jiaxin!
- Today I will present a fixed construction
  - On the negative side it is longer
  - On the positive side, the structure-preserving version is also  $O(\log Q)$ -tight
    - Previously it was only  $O(\lambda)$ -tight
  - The designated prover version is not impacted by this bug, so SPS is OK.
  - Ongoing work:
    - While working on the fixes, we could reduce the tight-SPS size from 12 to 10
  - Revised version will be updated in eprint soon



## CONSTRUCTION



 $\pi_0$  ,  $\pi_1$ Partition bit [Raf15] correct OR ·  $\rho$ ,  $\hat{\rho}$  correct  $\pi_3$ OR proof Fix

used to

introduce

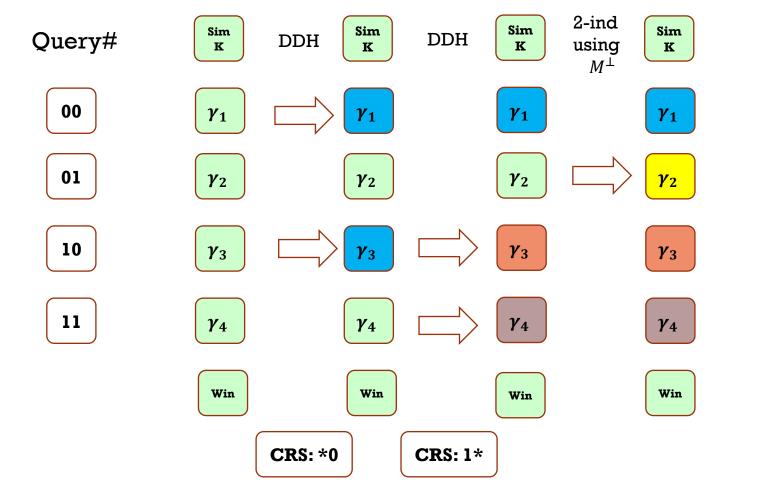
seed

randomness

into  $\gamma$ 

Inspired by [Hof17]

## PROOF STRATEGY



 $ho, \hat{
ho}, \gamma$ Encrypted QA-NIZK

 $\pi_0, \pi_1$ Partition bit correct
OR  $ho, \hat{
ho}$  correct



#### SUMMARY

- First USS-QA-NIZK where both CRS and proofs have number of group elements independent of the security parameter
- Shortest tightly secure SPS with 12 group elements under SXDH
  - Ongoing optimization work on 10 group elements
- Shortest public-verifiable tightly-secure CCA scheme
- Plugging our USS-QA-NIZK gives short tightly-secure primitives
  - Blind Structure-Preserving Signatures
  - Group Structure-Preserving Signatures
  - USS Groth-Sahai Proof System





Questions?